### Chapter 1

## Easy Problems

- 1.1.  $y = \tan x$
- 1.2.  $f(x) = g(x) \ln(g(x))$ .
- 1.3.  $y = \arctan x = \tan^{-1} x$
- 1.4.  $y = \arcsin(x)$
- 1.5.  $y = (x+1)\ln(x+1)$ .

#### Chapter 2

## **Probability Spaces**

- 2.1. A coin is weighted so that heads is four times as likely as tails. Find the probability that: (a) tails appears, (b) heads appears
- 2.2. Under which of the following functions does  $S = \{a_1, a_2\}$  become a probability space?
  - (a)  $P(a_1) = \frac{1}{3}$ ,  $P(a_2) = \frac{1}{2}$  (b)  $P(a_1) = \frac{3}{4}$ ,  $P(a_2) = \frac{1}{4}$ (c)  $P(a_1) = 1$ ,  $P(a_2) = 0$  (d)  $P(a_1) = \frac{5}{4}$ ,  $P(a_2) = -\frac{1}{4}$

# Appendix A

# Solutions

1.1

$$y = \tan x$$
  
=  $\frac{\sin x}{\cos x}$   
$$\frac{dy}{dx} = \frac{\cos x}{\cos x} + \sin x \times \frac{-1}{\cos^2 x} \times -\sin x$$
  
=  $1 + \tan^2 x$   
=  $\sec^2 x$ .

1.2

$$f'(x) = g'(x)\ln(g(x)) + \frac{g(x)}{g(x)}g'(x)$$
  
=  $g'(x)(1 + \ln(g(x))).$ 

1.3

$$\tan y = x$$

diff w.r.t. x:

$$\sec^2 y \frac{dy}{dx} = 1$$
$$\frac{dy}{dx} = \frac{1}{\sec^2 y}$$
$$= \frac{1}{1 + \tan^2 y}$$
$$= \frac{1}{1 + x^2}$$

1.4

$$\sin(y) = x$$

diff. w.r.t. x:

$$\cos y \frac{dy}{dx} = 1$$
$$\frac{dy}{dx} = \frac{1}{\cos y}$$
$$= \frac{1}{\sqrt{1 - \sin^2 y}}$$
$$= \frac{1}{\sqrt{1 - x^2}}.$$

1.5

$$\frac{dy}{dx} = \ln(x+1) + \frac{x+1}{x+1} \\ = 1 + \ln(x+1).$$

- 2.1 Let p = P(T), then P(H) = 4p. We require P(H) + P(T) = 1, so 4p + p = 1, hence  $p = \frac{1}{5}$ . Therefore: i.  $P(T) = \frac{1}{5}$ , ii.  $P(H) = \frac{4}{5}$
- $2.2\ 2.2\mathrm{b}$  and  $2.2\mathrm{c}$