THE MATHALFA PACKAGE

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The math alphabets normally addressed via the macros \mathcal, \mathbb, \mathfrak and \mathscr are in a number of cases not well-adapted to the IATEX math font structure. Some suffer from one or more of the following defects:

- font sizes are locked into a sequence that was appropriate for metafont—generated rather than scalable fonts;
- there is no option in the loading package to enable scaling;
- the font metrics are designed for text rather than math mode, leading to awkward spacing, subscript placement and accent placement when used for the latter;
- the means of selecting a set of math alphabets varies from package to package.

The goal of this package is to provide remedies for the above, where possible. This means, in effect, providing virtual fonts with my personal effort at correcting the metric issues, rewriting the font-loading macros usually found in a .sty and/or .fd files to admit a scale factor in all cases, and providing a .sty file which is extensible and from which any such math alphabet may be specified using a standard recipe.

For example, the following fonts are potentially suitable as targets for \mathcal or \mathcal or \mathcal are either included as part of TeXLive 2011, as free downloads from CTAN or other free sources, or from commercial sites.

```
cm % Computer Modern Math Italic (cmsy)
euler % euscript
rsfs % Ralph Smith Formal Script---heavily sloped
rsfso % based on rsfs, much less sloped
lucida % From Lucida New Math (commercial)
mathpi % Adobe Mathematical Pi or clones thereof (commercial)
mma % Mathematica fonts
pxtx % pxfonts/txfonts
mt % Mathtime (commercial)
mtc % Mathtime Curly (commercial)
zapfc % Adobe Zapf Chancery (URW clone is part of TeXLive)
esstix % ESSTIX-thirteen
boondox % calligraphic alphabet derived from stix fonts
boondoxo % based on boondox, but less oblique
dutchcal % regular and bold weights derived from ESSTIX13
```

Once you have installed the support packages for these fonts and the mathalfa package, you may select a particular calligraphic font for \mathcal using something like

\usepackage[cal=rsfso,calscaled=.96]{mathalfa}

which loads rsfso at 96% of natural size as the math calligraphic alphabet. You may at the same time select the output for \mathbb, \mathfrak, \mathbfrak (since the Mathematica fonts have a bold version of bb) and \mathscr with

```
\usepackage[cal=mathpi,
calscaled=.94,
bb=ams,
frak=mma,
frakscaled=.97,
scr=rsfs]{mathalfa}
```

As initially configured, mathalfa makes available the following options:

cal=: Select the calligraphic alphabet from the list above.

calscaled=: Select a scale factor for cal.

scr=: Select the script alphabet from rsfs, rsfso, euler, lucida, mathpi, mma, mtc, zapfc, esstix, boondox, boondoxo. dutchcal, pxtx.

scrscaled=: Select a scale factor for **scr**.

frak=: Select the fraktur alphabet from euler, lucida, mathpi, mma, mt, esstix, boondox, pxtx.

frakscaled=: Select a scale factor for frak.

bb=: Select the Blackboard bold alphabet from ams, lucida, mathpi, mma, mt, mth, pazo, fourier, esstix, boondox, px, tx, txof.

bbscaled=: Select a scale factor for bb.

scaled=: Select a scale for all alphabets chosen within mathalfa.

showoptions: This option throws an error and shows a list of all installed option values for bb, cal, frak and scr on the console.

Notes

- If bold versions exist, they are loaded and may be used with the macros \mathbcal, \mathbbb, \mathbfrak and \mathbcal.
- If you prefer that the bold weight be the default target from \mathcal, enter

\let\mathcal\mathbcal

after loading the mathalfa package. (You may find this a useful option if you specified cal=dutchcal, as that font is quite light.)

 Use of zapfc as a value for either cal or scr requires that you install the urwchancal package from

http://ctan.tug.org/tex-archive/fonts/urwchancal. (It is distributed as part of T_FX Live as of March 2011.)

• Use of the rsfso as a value for either cal or scr requires that you install the rsfso package from

http://ctan.tug.org/tex-archive/fonts/rsfso. (It is distributed as part of TFX Live as of March 2011.)

• Use of mma as a value requires that you download and install the fonts from http://support.wolfram.com/technotes/latestfonts.en.html.

The support files may be downloaded from

http://phong.informatik.uni-leipzig.de/~kuska/.

In particular, wolfram.map must be enabled. Virtual fonts with metrics that are suitable for math mode are also required. A TDS with the required files (including virtual fonts with tuned metrics) is available at

http://public.me.com/mjsharpe/mmaTDS.zip.

- Use of mathpi requires that you purchase and install the Adobe Mathematical Pi fonts (#2 and #6) or clones thereof. If you choose to buy them, you may download support files, including virtual fonts with tuned metrics, from http://public.me.com/mjsharpe/mathpiTDS.zip.
- The pxtx package consists of virtual fonts drawn from the math alphabets in the pxfonts and txfonts packages, with modified metrics. The calligraphic fonts are identical to those in the Mathematica package, but the others seem distinct. The pxtx package is part of TeX Live.
- The Adobe Bickham Script Pro font collection in opentype format is rather expensive but quite elegant. Its upper-case glyphs are well-suited for adaptation as a math calligraphic font once the slant is reduced. The bickham package makes available virtual fonts and LATEX support files for these fonts, and can be used as the target for \mathcal and \mathcal and \mathcal as well as their bold variants.
- The ESSTIX collection is a creation of Elsevier Publishing in 2000, though never officially released by them. Before development was complete, the collection was donated to the STIX math font project, to which it seems to have been a precursor. Distribution has since been deprecated, but in my opinion, math alphabet fonts, especially math script fonts, are so rare that none should be allowed to become extinct. The BlackBoard Bold ESSTIX font (ESSTIX14) is close to both the mathpi and Fourier Blackboard Bold fonts, and the fraktur ESSTIX font (ESSTIX15) is similar to mathpi fraktur. However, the ESSTIX script font (ESSTIX13) seems to be a distinct and interesting face. The PostScript versions of these fonts have been hard to find, but the TrueType versions may be found embedded within the Amaya project, available at

http://www.w3.org/Amaya/.

The ESSTIX PostScript fonts, virtual math fonts and LaTeX support files may be downloaded now from

http://mirror.ctan.org/fonts/esstix.

This provides virtual fonts with tfm names esstixcal, esstixbb and esstixfrak. As of May 2011, the esstix package is distributed as a part of T_FX Live.

• The STIX fonts are currently (May 2011) distributed only in OpenType format. The Post-Script BOONDOX fonts (in the USA, the boondocks and the sticks are essentially synonymous) containing their calligraphic, fraktur and double-struck (blackboard bold) alphabets in regular and bold weights were manufactured from STIX .otf fonts using FontForge. Virtual fonts were then created using fontinst to customize the metrics for positioning accents and subscripts. A TDS package with the fonts and support files may be downloaded from http://mirror.ctan.org/fonts/boondox.

The following are my opinions. No objective judgment should be inferred.

• If your interest in math fonts goes beyond the basic level, you should look into the commercial products Lucida from http://www.tug.org/store/lucida/order.html and Mathtime

Pro 2 from http://pctex.com. Both are high quality products, and are excellent values for the prices. Even if you only use small pieces of the collections, these are much better buys than most commercial text fonts.

- The Mathematica fonts are not of very high quality as a collection, but they have some good parts. In particular, the calligraphic math font may be turned into a useful target for \mathcal after its metrics have been fine-tuned. You are missing out on some good stuff if you don't install this free collection.
- The txfonts and pxfonts packages provide a number of math alphabets that deserve more attention—the fraktur in particular is quite handsome but should perhaps be scaled up a bit.
- The rsfs package is not suitable for \mathcal, being much too slanted. The best options for \mathcal are rsfso, esstix, boondoxo and mt, the latter requiring the (non-free) mtpro2 collection.
- If you own the mtpro2 collection, look into the 'curly' script font, which seems useful, though a bit heavy.
- It is questionable whether there is value in the Mathpi fonts given that there are free close approximants to each of them.
- The STIX (BOONDOX) calligraphic font is quite handsome. I prefer it to be less sloped, along the lines of rsfso. This is provided by the option boondoxo, which provides virtual fonts sloped approximately like rsfso.

HEIGHT COMPARISONS:

The CapHeight of a font is supposed to represent the height of capital letters in the font in units where 1000 is equal to 1em, the size of \quad which, for a font of nominal size 10pt is in most cases equal to 10pt. Script fonts often have irregularly sized capital letters, and the CapHeight should perhaps represent the median height of capitals. This is not always so. For example, pzc (Adobe Zapf Chancery) and uzc (its URW clone) have the same glyph metrics, but their CapHeights are listed respectively as 708 and 573. These numbers, taken from their AFM files, represent in the first case the second greatest height of capital letters and the second case the second smallest. If the CapHeight is to provide useful information about scaling the font, a more central value is 595, indicating that in most cases, Zapf Chancery usually needs to be scaled up by about 15%.

For the purpose of making scale factors to mediate between these disparate fonts, the following chart may be helpful.

Computer Modern Roman (cmr10)	683
Zapf Chancery (pzcmi/uzcmi)	595
Euler fraktur(eufm10)	690
Euler script(eusm10)	695
rsfs/rsfso	710
Computer Modern calligraphic (cmsy10)	703
Mathpi calligraphic (mh2scr)	720
Mathpi fraktur (mh2)	762
Mathpi Blackboard bold (mh6)	720
pxtx calligraphic (txr-cal)	684
pxtx calligraphic-bold (txb-cal)	684
pxtx fraktur (txr-frak)	684
pxtx fraktur-bold (txb-frak)	679
pxtx openface (tx-of)	664
pxtx openface-bold (txr-of)	678
tx double-struck (txr-ds)	684
px double-struck (pxr-ds)	693
px double-struck-bold (pxb-ds)	698
bickham calligraphic (bickham-r)	683
Lucida calligraphic (lbms)	723
Lucida Blackboard bold (lbma)	723
Lucida fraktur (lbl)	741
mtpro2 calligraphic (mt2mst)	702
mtpro2 curly (mt2mct)	702
mtpro2 Blackboard bold (mt2bbt)	690
mtpro2 Holey Roman (mt2hrbt)	690
Mathematica calligraphic (Mathematica5)	685
Mathematica fraktur (Mathematica6)	690
Mathematica Blackboard bold (Mathematica7)	662
Mathpazo Blackboard bold (fplmbb)	692
Fourier Blackboard bold (fourier-bb)	693
ESSTIX Calligraphic (ESSTIX13)	692
ESSTIX Blackboard bold (ESSTIX14)	696
ESSTIX fraktur (ESSTIX15)	700
BOONDOX Calligraphic	687
BOONDOX Blackboard bold	662
BOONDOX fraktur	695

Here are some samples from the fonts mentioned above:

Fraktur:

euler (Euler fraktur):

ABCDEFGSNNNDPQRSTUVWXY3
mma (Mathematica fraktur):

A B C D \in F G H I J K L M N O P Q R S T U V W X Y Z lucida (Lucida fraktur):

ABCDEFGSSNNDPQRSTUVWXY3
mma (Mathematica fraktur-bold):

MBCDG KGSXXXX MNDBQ HGTUBWXY3
boondox (BOONDOX fraktur-bold):

UPRIGHT:

euler (Euler script):

 ${\cal A} \ \, {\cal B} \ \, {\cal C} \ \, {\cal D} \ \, {\cal E} \ \, {\cal F} \ \, {\cal G} \ \, {\cal H} \ \, {\cal J} \ \, {\cal J} \ \, {\cal K} \ \, {\cal L} \ \, {\cal M} \ \, {\cal N} \ \, {\cal O} \ \, {\cal P} \ \, {\cal Q} \ \, {\cal R} \ \, {\cal S} \ \, {\cal T} \ \, {\cal U} \ \, {\cal V} \ \, {\cal W} \ \, {\cal X} \ \, {\cal Y} \ \, {\cal Z}$ euler (Euler script-bold):

RESTRAINED:

cm (CM calligraphic, cmsy):

 ${\mathcal A} \ {\mathcal B} \ {\mathcal C} \ {\mathcal D} \ {\mathcal E} \ {\mathcal F} \ {\mathcal G} \ {\mathcal H} \ {\mathcal I} \ {\mathcal I} \ {\mathcal K} \ {\mathcal L} \ {\mathcal M} \ {\mathcal N} \ {\mathcal O} \ {\mathcal P} \ {\mathcal Q} \ {\mathcal R} \ {\mathcal S} \ {\mathcal T} \ {\mathcal U} \ {\mathcal V} \ {\mathcal W} \ {\mathcal X} \ {\mathcal Y} \ {\mathcal Z}$ lucida (Lucida calligraphic):

 \mathcal{A} \mathcal{B} \mathcal{C} \mathcal{D} \mathcal{E} \mathcal{F} \mathcal{G} \mathcal{H} \mathcal{I} \mathcal{J} \mathcal{K} \mathcal{L} \mathcal{M} \mathcal{N} \mathcal{O} \mathcal{P} \mathcal{Q} \mathcal{R} \mathcal{S} \mathcal{T} \mathcal{U} \mathcal{V} \mathcal{W} \mathcal{X} \mathcal{Y} \mathcal{Z}

mma (Mathematica script-bold):

 $\mathcal{A} \ \mathcal{B} \ \mathcal{C} \ \mathcal{D} \ \mathcal{E} \ \mathcal{F} \ \mathcal{G} \ \mathcal{H} \ I \ \mathcal{J} \ \mathcal{K} \ \mathcal{L} \ \mathcal{M} \ \mathcal{N} \ \mathcal{O} \ \mathcal{P} \ \mathcal{Q} \ \mathcal{R} \ \mathcal{S} \ \mathcal{T} \ \mathcal{U} \ \mathcal{V} \ \mathcal{W} \ \mathcal{X} \ \mathcal{Y} \ \mathcal{Z}$ pxtx (pxtx script):

 \mathcal{A} \mathcal{B} \mathcal{C} \mathcal{D} \mathcal{E} \mathcal{F} \mathcal{G} \mathcal{H} \mathcal{I} \mathcal{J} \mathcal{K} \mathcal{L} \mathcal{M} \mathcal{N} \mathcal{O} \mathcal{P} \mathcal{Q} \mathcal{R} \mathcal{S} \mathcal{T} \mathcal{U} \mathcal{V} \mathcal{W} \mathcal{X} \mathcal{Y} \mathcal{Z} pxtx (pxtx script-bold):

 $\mathcal{A} \ \mathcal{B} \ \mathcal{C} \ \mathcal{D} \ \mathcal{E} \ \mathcal{F} \ \mathcal{G} \ \mathcal{H} \ I \ \mathcal{J} \ \mathcal{K} \ \mathcal{L} \ \mathcal{M} \ \mathcal{N} \ \mathcal{O} \ \mathcal{P} \ \mathcal{Q} \ \mathcal{R} \ \mathcal{S} \ \mathcal{T} \ \mathcal{U} \ \mathcal{V} \ \mathcal{W} \ \mathcal{X} \ \mathcal{Y} \ \mathcal{Z}$ EMBELLISHED:

mt (Mathtime Pro 2 script):

A B C D & F S H I J K L M N O P Q R S T U V W X Y Z mathpi (Mathpi script):

 $\mathcal{A} \ \mathcal{B} \ \mathcal{C} \ \mathcal{D} \ \mathcal{E} \ \mathcal{F} \ \mathcal{G} \ \mathcal{H} \ \mathcal{G} \ \mathcal{G} \ \mathcal{K} \ \mathcal{L} \ m \ n \ \varnothing \ \mathcal{P} \ \mathcal{Q} \ \mathcal{R} \ \mathcal{S} \ \mathcal{T} \ \mathcal{U} \ \mathcal{V} \ \mathcal{W} \ \mathcal{X} \ \mathcal{Y} \ \mathcal{Z}$ dutchcal (dutchcal calligraphic):

 $\mathcal{A} \ \mathcal{B} \ \mathcal{C} \ \mathcal{D} \ \mathcal{E} \ \mathcal{F} \ \mathcal{G} \ \mathcal{H} \ \mathcal{G} \ \mathcal{G} \ \mathcal{K} \ \mathcal{L} \ m \ n \ \odot \ \mathcal{P} \ \mathcal{Q} \ \mathcal{R} \ \mathcal{S} \ \mathcal{T} \ \mathcal{U} \ \mathcal{V} \ \mathcal{W} \ \mathcal{X} \ \mathcal{Y} \ \mathcal{Z}$ dutchcal (dutchcal calligraphic-bold):

 $\mathcal{A} \ \mathcal{B} \ \mathcal{C} \ \mathcal{D} \ \mathcal{E} \ \mathcal{F} \ \mathcal{G} \ \mathcal{H} \ \mathcal{G} \ \mathcal{F} \ \mathcal{L} \ m \ n \ \Theta \ \mathcal{P} \ \mathfrak{Q} \ \mathcal{R} \ \mathcal{S} \ \mathcal{T} \ \mathcal{U} \ \mathcal{V} \ \mathcal{W} \ \mathcal{X} \ \mathcal{Y} \ \mathcal{Z}$ bickham (bickham calligraphic):

ABCDEFGHIJKLMNODQQQWXYZ rsfso:

A R C D E F G H F J R L M N 6 P Q R S T U V W X Y E boondoxo (BOONDOX Calligraphic Oblique-bold):

A B C D C F G H J J K L M N O P Q R S T U V W X Y E HEAVILY SLOPED:

boondox (BOONDOX Calligraphic):

ABCDEFEHJJKLMNOFQRSTUVWXYZ rsfs:

Double-Struck (Blackboard Bold):

HOLLOWED-OUT SHAPES:

ams (AMS bb):

 $\mathbb{A} \ \mathbb{B} \ \mathbb{C} \ \mathbb{D} \ \mathbb{E} \ \mathbb{F} \ \mathbb{G} \ \mathbb{H} \ \mathbb{I} \ \mathbb{J} \ \mathbb{K} \ \mathbb{L} \ \mathbb{M} \ \mathbb{N} \ \mathbb{O} \ \mathbb{P} \ \mathbb{Q} \ \mathbb{R} \ \mathbb{S} \ \mathbb{T} \ \mathbb{U} \ \mathbb{V} \ \mathbb{W} \ \mathbb{X} \ \mathbb{Y} \ \mathbb{Z}$ mth (Mathtime Pro 2 Holey Roman):

 $\mathbb{A} \ \mathbb{B} \ \mathbb{C} \ \mathbb{D} \ \mathbb{E} \ \mathbb{F} \ \mathbb{G} \ \mathbb{H} \ \mathbb{I} \ \mathbb{J} \ \mathbb{K} \ \mathbb{L} \ \mathbb{M} \ \mathbb{N} \ \mathbb{O} \ \mathbb{P} \ \mathbb{Q} \ \mathbb{R} \ \mathbb{S} \ \mathbb{T} \ \mathbb{U} \ \mathbb{V} \ \mathbb{W} \ \mathbb{X} \ \mathbb{Y} \ \mathbb{Z}$ mth (Mathtime Pro 2 Holey Roman-bold):

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z txof (tx of bold):

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z GEOMETRIC SHAPES:

lucida (Lucida bb):

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z mathpi (Mathpi bb):

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z mma (Mathematica bb):

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z pazo (Mathpazo bb):

 $\begin{picture}(20,10) \put(0,0){\mathbb{R}} \put($

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z px (px bb):

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z fourier (Fourier bb):

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z esstix (ESSTIX bb):

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z boondox (BOONDOX bb):

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z boondox (BOONDOX bb-bold):

 ${\Bbb C}$ ${\Bbb D}$ ${\Bbb H}$ ${\Bbb N}$ ${\Bbb P}$ ${\Bbb Q}$ ${\Bbb R}$ ${\Bbb Z}$ (few glyphs available.)

mt (Mathtime Pro 2 bb-bold):

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z mma (Mathematica bb-bold):

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z

Notes:

- Lucida fonts generally need to be reduced in scale to match other math and text fonts.
- Zapf Chancery need to be scaled up by 15% or so. This font is not really suited for use as a math alphabet due to the disparate heights and depths and the long tails on some glyphs. Use with care.
- Mathematica fraktur is quite readable, but not very attractive, seeming to have random variations in baseline and height. It's also a bit too heavy to be a good match to most other fonts. Similar comments could apply to Lucida fraktur, which has a very distinctive appearance with some features more similar to Duc de Berry than to other fraktur fonts.
- The calligraphic fonts break down into four natural groups—(i) the upright styled Euler and Curly; (ii) the less-embellished CM, Lucida, Zapf Chancery, ESSTIX, dutchcal, Mathematica and pxtx; (iii) the moderately sloped but more embellished Mathpi, Mathtime, bickham, rsfso and boondoxo; (iv) the heavily sloped rsfs and the slightly less sloped boondox. My preference, if not using mathtime or lucida, is to set \mathcal to one from group (ii) and \mathscr to one from group (iii).
- Blackboard bold can look poor in some cases. In my opinion, AMS bb and some of the others show up as ghostly (gray and indistinct) especially on the screen and may not appear to match the weights of other math glyphs. (AMS bb, Mathtime Pro 2 Holey Roman and the txof bb fonts appear to be formed by removing the interiors of solid glyphs from a bold, serifed font. Mathtime Pro 2 Holey Roman Bold is a much better fit to most math fonts of weight heavier than Computer Modern.) Fourier, Mathpi, ESSTIX and boondox bb appear to be very close in style, with mathpi bb a bit less sharp. Mathpazo bb, Mathematica bb, px bb and tx bb have a heavier appearance and should work better with fonts other than Computer Modern.

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